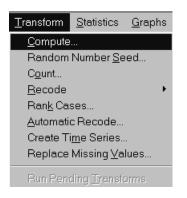
BREAKDOWN TIMES

12. Linear Regression Analysis with SPSS

In this section we will demonstrate how to apply the linear regression procedure in SPSS to the insulating fluid data. The numerical outputs and graphical displays for the data were discussed in Sections 6 and 7.

As the simple linear regression model will be used for the log-transformed times to breakdown, we will demonstrate first how to carry out the transformation with SPSS. Click on *Transform* in the menu and then on *Compute*...



The *Compute Variable* dialog box is displayed. In the *Target Variable* box enter the name of the new variable as *lntime*. Transfer the natural logarithm function LN from the *Functions* box to the *Numeric Expression* box by clicking on the function name and then on >. Then move in the same way the variable *time* to the *Numeric Expression* box. The dialog box should have the following form:

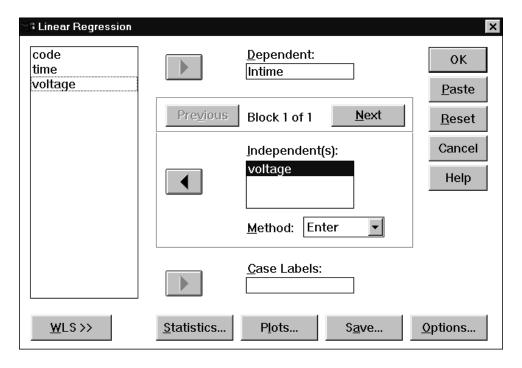
Compute Variable	X
Target Variable: Numeric Expression: Intime = Type&Label Image code + time + voltage + - <=	×
OK Paste Reset Cancel Help	

Click on OK. As a result, the new variable *lntime* is obtained in one of the columns of the data file. Now we are ready to carry out the simple linear regression with lntime as the dependent variable and *Voltage* as the explanatory variable.

In order to access the simple linear regression procedure in SPSS, choose *Statistics* and then *Regression*. The following menu will be displayed:

<u>S</u> tatistics <u>G</u> raphs <u>U</u> til	ities <u>W</u> indow <u>H</u> elp
S <u>u</u> mmarize Custom <u>T</u> ables Compare <u>M</u> eans ANO <u>V</u> A Models Correlate	k.sav
— <u>R</u> egression L <u>o</u> glinear Classify <u>D</u> ata Reduction	
Sc <u>a</u> le <u>N</u> onparametric Tests Time Series <u>S</u> urvival Mu <u>l</u> tiple Response	

Click on *Linear* to open the *Linear Regression* dialog box. The four variable names *code*, *lntime*, *time*, *voltage* will appear in the left-hand box. In this case the dependent variable is *lntime* and the independent variable is *voltage*. Transfer these variables names into appropriate boxes in the dialog box by clicking on the variable name and then on >.



Click on *Statistics...* tab to obtain statistics for the linear regression. *Estimates* of the regression coefficients and *Model fit* are default options. In order to obtain the mean and standard deviation for each variable, and a correlation matrix, check *Descriptives* box. It is also very useful to obtain the 95% confidence intervals for the regression coefficients.

Linear Regression: Statistics		×
Regression Coefficients	☑ Descriptives	Continue
☑ <u>E</u> stimates	⊠ <u>M</u> odel fit	Cancel
☑ Confidence intervals	□ <u>B</u> lock summary	Cancer
□ Co <u>v</u> ariance matrix	□ D <u>u</u> rbin-Watson	Help
	□ Collinearity diagnostics	

Click on *Continue* to return to the *Linear Regression* dialog box. Information about residuals is obtained by clicking on the *Plots* tab. *Linear Regression: Plots* dialog box opens.

Linear Regression: Plots		×
DEPENDNT *ZPRED *ZRESID *DRESID *ADJPRED *SRESID *SDRESID	Previous Scatter 1 of 1 Next Y:	Continue Cancel Help
□ <u>P</u> roduce all partial p	lots	
☐ Standardized Reside	ial Plots	
□ <u>H</u> istogram	₽ <u>C</u> asewise plot	
□ No <u>r</u> mal probability	plot <u>©</u> utliers outside <u>3</u> std. o <u>A</u> ll cases	deviations

Plots can aid in the validation of the assumptions of normality, linearity, and equality of variances. Plots also allow you to check whether there are any cases, which might be considered as outliers and so dropped from the analysis. Click on the *Casewise plot* check box to obtain a listing of any exceptionally large residuals. We recommend that this is done for an initial run of the procedure. Click on *Continue* and the on OK to run the regression for the first time.

No outliers have been found in the insulating fluid data. The listing states: *No outliers found. No casewise plot produced.*

Now we can request a plot of residuals against the predicted values. The plot allows you to check whether the assumption of constant variance is not violated. We then look for a change in the spread or dispersion of the plotted points.

SPSS creates several temporary variables (prefaced with *) during execution of a regression analysis. *PRED comprises the unstandardized predicted values, *RESID is the set of unstandardized residuals, *ZPRED contains the standardized predicted values (i.e. *PRED has been transformed to a scale with mean 0 and standard deviation of 1), and *ZRESID comprises the standardized residuals (i.e. *RESID standardized to a scale with mean 0 and standard deviation of 1).

In order to obtain a plot of residuals against the predicted values, click on *ZRESID and then on > to transfer the variable to the Y: box, and on *ZPRED and then on > to transfer the variable to the X: box. The completed *Linear Regression: Plots* dialog box is shown below.

DEPENDNT *ZPRED *ZRE SID *DRE SID *ADJPRED *SRE SID *SDRE SID *SDRE SID *SDRE SID	Linear Regression: Plots		×	
Standardized Residual Plots	*ZPRED *ZRESID *DRESID *ADJPRED *SRESID *SDRESID	Y: *ZRESID X: *ZPRED	Cancel	
● <u>A</u> ll cases		ty plot ©utliers outside 3 std.	deviations	

The normality assumption can be verified by looking at the plot of residuals. In order to assess whether the normality assumption is not violated with SPSS, the normal P-P plot of regression standardized residuals is obtained. The plot plots the cumulative proportions of standardized residuals against the cumulative proportions of the normal distribution. If the normality assumption is not violated, points will cluster around a straight line. In order to obtain the plot, check the *Normal probability plot* box.

Click on *Continue* to return to the *Linear Regression* dialog box. Click on *Save...* to save predicted values, residuals, and other statistics useful for diagnostics. Each selection adds one or more new variables to your active data file. In particular, the predicted values (mean estimates) are obtained as the variables pre_1 and sep_1, respectively. The *Linear Regression: Save New Variables* dialog box is displayed below.

Linear Regression: Save Ne w Variables		×
Predicted Values ✓ Unstandardized □ Standardized	Residuals IF U <u>n</u> standardized I∏ St <u>a</u> ndardized IF Obviounting d	Continue Cancel Help
□ Adjusted ☑ S.E. of mean <u>p</u> redictions □ Distances	□ <u>S</u> tudentized □ <u>D</u> eleted □ Studentized de <u>l</u> eted	пер
□ <u>M</u> ahalanobis □ Coo <u>k</u> 's □ Le <u>v</u> erage values	□Influence Statistics □Df <u>B</u> eta(s) □Standardi <u>z</u> ed DfBeta(s)	
Prediction Intervals ☑ M <u>e</u> an ☑ Individual <u>C</u> onfidence Interval: 95 %	□ Df <u>F</u> it □ Standardized DfFi <u>t</u> □ C <u>o</u> variance ratio	

Click on *Continue* to return to the *Linear Regression* dialog box. Click on *OK* to obtain the linear regression output. The numerical output is discussed in **Section 6.** The plots obtained to validate the assumptions of the linear regression model are discussed in **Section 7**.