

Ex 2-1:

$H_0 : \mu = 150$ vs $H_1 : \mu > 150$

Population standard deviation σ is given and equal to 3 ($\sigma = 3$)

Hence, the test statistic is given by

$$Z = \frac{\bar{y} - \mu_0}{\sigma / \sqrt{n}}$$

$$\bar{y} = 148.75$$

Computed value $z_0 = -0.8333$.

b). The rejection region corresponding to $\alpha = 0.05$ (one-sided) is any value of z_0 larger than or equal to 1.645.

Since, the computed value $z_0 = -0.8333$ is not larger than 1.645, do not reject the null hypothesis.

c). P-value is the area to the right of -0.8333 under standard normal curve, which is larger than 0.796.

d). 95% confidence interval on μ :

$$\bar{y} \pm 1.96\sigma / \sqrt{n}$$

which leads to $[148.75 \pm 1.96 * 1.5]$.

Ex-2-3

$H_0 : \mu = 0.255$ vs $H_1 : \mu \neq 150$

Population standard deviation σ is given and equal to 0.0001 ($\sigma = 3$)

Hence, the test statistic is given by

$$Z = \frac{\bar{y} - \mu_0}{\sigma / \sqrt{n}}$$

$$n=10$$

$$\bar{y} = 0.2545$$

Computed value $z_0 = 15.81139$

b). The rejection region corresponding to $\alpha = 0.05$ (two-sided) is any value of $|z_0|$ larger than or equal to 1.96.

Since, the computed value $z_0 = 15.81139$ is larger than 1.645, reject the null hypothesis.

c). P-value is the area to the right of 15.81139 plus the area to the left of -15.81139 under standard normal curve (in view of two-sided alternative), which is lvery much smaller than 0.001.

d). 95% confidence interval on μ :

$$\bar{y} \pm 1.96\sigma / \sqrt{n}$$

which leads to $[0.255 \pm 1.96 * 0.00003162278] = [0.255 \pm 0.00006198064]$.

Ex2-5:

a). $H_0 : \mu = 120$ vs $H_1 : \mu > 120$

b). Population standard deviation σ is unknwn. Hence the test statistic is given by

$$t = \frac{\bar{y} - \mu_0}{s / \sqrt{n}}, \text{ with } n-1 \text{ degrees of freedom and } n=10.$$

$$\bar{y} = 131 \text{ and } s = 19.54482$$

$t_0 = 1.7798$, $df = 9$. The rejection region at $\alpha = 0.01$ is given by region with any value of t_0 larger (one sided) than 2.821.

Since, the computed value $t_0 = 1.7798$ is not larger than 2.821 do not reject H_0 at $\alpha=0.01$.

c). One-sided alternative H_1 . Hence, the p-value is the area to the right of 1.7798 under student-t curve with 9 d.f which gives p-value = 0.0544.

d). 99 percent confidence interval: $[110.914, 151.086]$.

Ex2-11:2

a). $H_0 : \sigma_1^2 = \sigma_2^2$ vs $H_1 : \sigma_1^2 \neq \sigma_2^2$

Test statistics: $F = \frac{S_1^2}{S_2^2}$. When H_0 is true the distribution of this test statistic is F with $\nu_1 = 9$ and

$v_2 = 9$.

From the data, $s_1^2 = 85.822222$ and $s_2^2 = 87.733333$. Since, s_2^2 is larger than s_1^2 we compute $F = \frac{s_2^2}{s_1^2}$ (which guarantees F to be larger than 1).

$$F_0 = 1.022268.$$

From table, the critical value for $\alpha = 0.05$ of F with $v_1 = 9$ and $v_2 = 9$ is 3.23.

Since the computed value, F_0 is not larger than the critical value, 3.23 do not reject the null hypothesis at 5% level of significance.

p-value is larger than 0.5.

b). $H_0 : \mu_1 = \mu_2$ vs $H_1 : \mu_1 \neq \mu_2$

Test statistic:

$$t = \frac{\bar{y}_1 - \bar{y}_2}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

where $n_1 = 10 = n_2$ and s_p is the pooled standard deviation (see equation 2-25 in your text)

$t_0 = 0.048$, with $df = 18$, p-value = 0.9622.

Do not reject H_0 at 5% level of significance.

Ex2-12

a) and b). $H_0 : \mu_1 = \mu_2$ vs $H_1 : \mu_1 \neq \mu_2$

Test statistic:

$$t = \frac{\bar{y}_1 - \bar{y}_2}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

where $n_1 = 6 = n_2$.

$t = -1.3498$, $df = 10$, p-value = 0.2068

For $\alpha = 0.05$ do not reject H_0 .

c). $H_0 : \sigma_1^2 = \sigma_2^2$ vs $H_1 : \sigma_1^2 \neq \sigma_2^2$

$s_1^2 = 0.674667$ and $s_2^2 = 0.577667$

$F_0 = 1.167917$ with $v_1 = 5$ and $v_2 = 5$

The critical value at $\alpha = 0.05$, is 5.05. Hence, do not reject H_0 .

P-value is given by the area to right of 1.167917 under F-curve with $v_1 = 5$ and $v_2 = 5$ which is larger than 0.5 and hence do not reject H_0 .